





JC-2017-49

19 December 2022

PRIIPs – Flow diagram for the risk and reward calculations in the PRIIPs KID

1. Introduction

The diagrams below set out the calculation steps for the Summary Risk Indicator (market risk and credit risk assessment) and Performance Scenario calculations described in Commission Delegated Regulation (EU) 2017/653.

They are being published as part of the Question and Answer (Q&A) material developed by the European Supervisory Authorities (ESAs) on the application of the requirements for the PRIIPs KID as practical convergence tools used to promote common supervisory approaches and practices in accordance with Article 29(2) of the ESA Regulations.

The diagrams are of a non-binding nature and do not constitute professional or legal advice. The legal requirements that need to be compiled with are those in Commission Delegated Regulation (EU) 2017/653 and not the text included in these diagrams. Please also be aware that the ESAs could adopt a formal position, which is different from the one expressed in this document.

All article references are to Commission Delegated Regulation (EU) 2017/653 unless otherwise stated.

The ESAs will review this document periodically or based on questions or comments from external stakeholders and updates are expected over time. In particular, please note that this document does not reflect the amendments to the requirements for the Summary Risk Indicator and Performance scenarios in Commission Delegated Regulation (EU) 2021/2268 that are applicable from 1 January 2023. The ESAs are currently working on an updated version of this document that will be published in due course.

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3. Acronyms used

CQS Credit Quality Step

CRM Credit Risk Measure

ECAI External Credit Assessment Institution

ESAs European Supervisory Authorities

EXP Exponential

KID Key Information Document

MRM Market Risk Measure

OTC Over The Counter

PCA Principal Component Analysis

PRIIP Package Retail and Insurance-based Investment Product

Q&A Question and Answer

RHP Recommended Holding Period

SRI Summary Risk Indicator

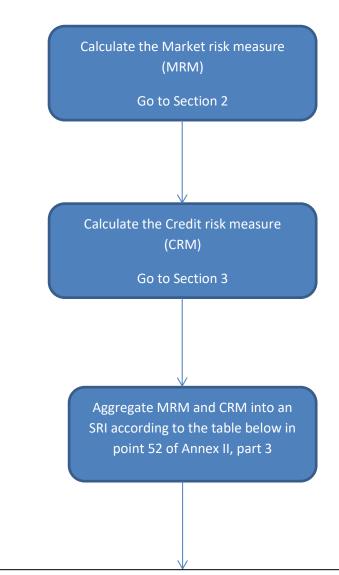
VaR Value-at-risk

VEV VaR-Equivalent Volatility

4. Flow Diagrams

A. Summary Risk Indicator (SRI)

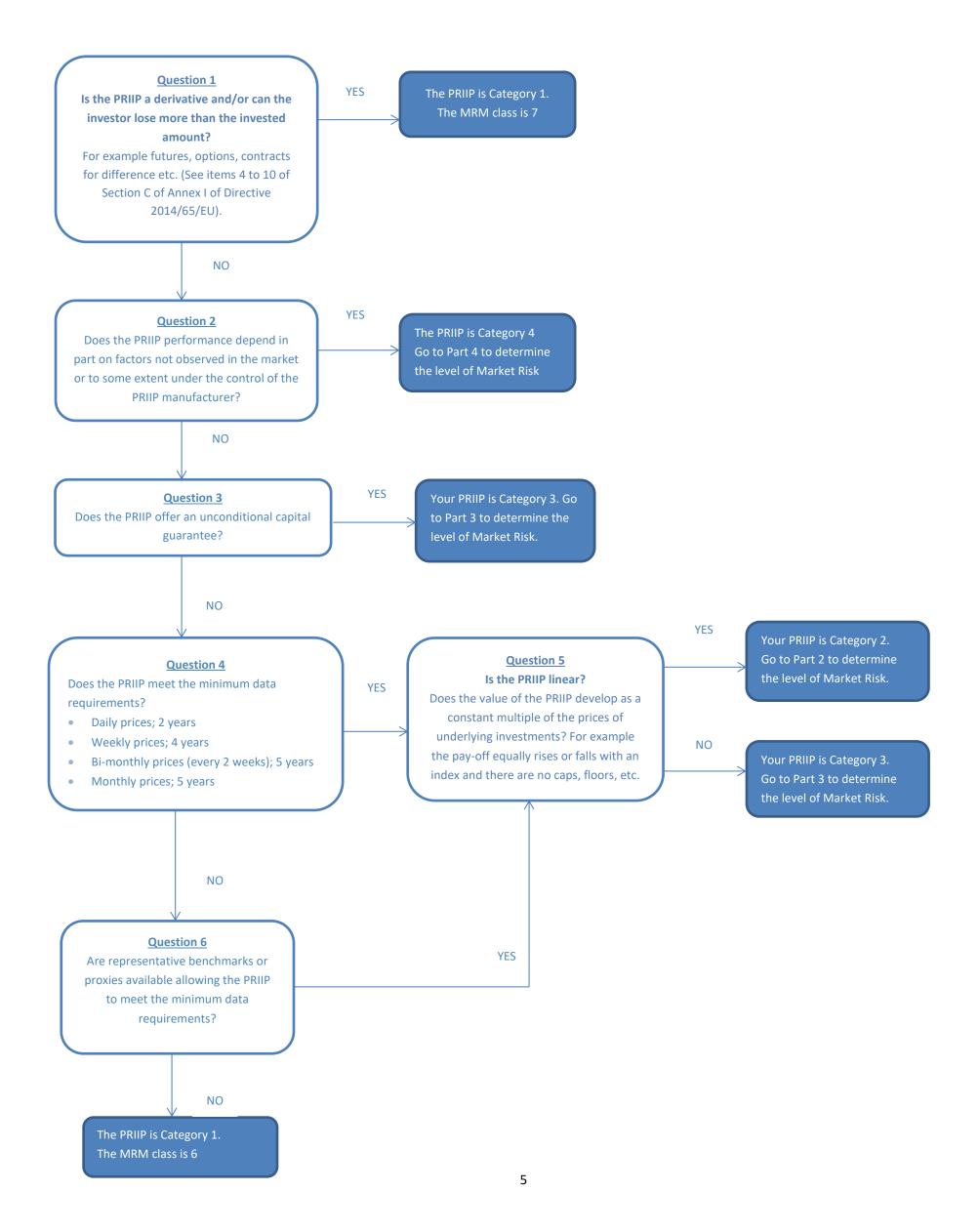
Section 1: Calculating the Summary Risk Indicator

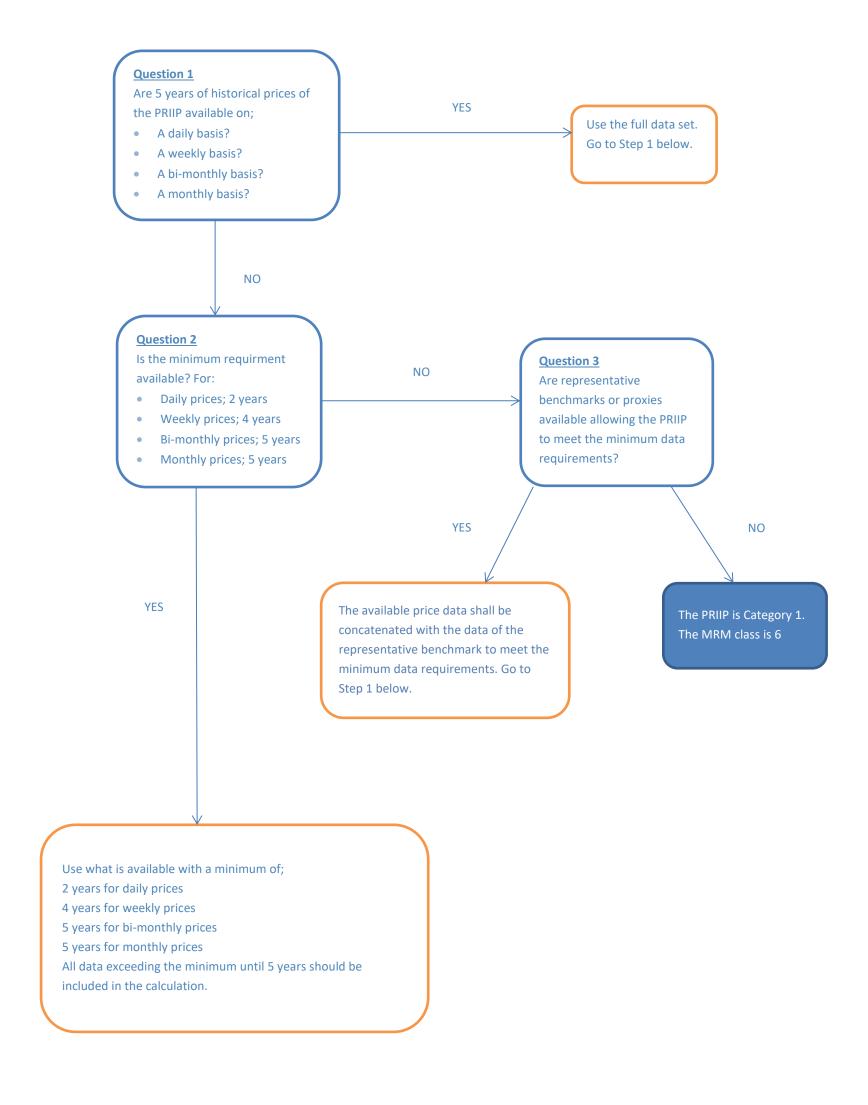


CRM class	MR1	MR2	MR3	MR4	MR5	MR6	MR7
CR1	1	2	3	4	5	6	7
CR2	1	2	3	4	5	6	7
CR3	3	3	3	4	5	6	7
CR4	5	5	5	5	5	6	7
CR5	5	5	5	5	5	6	7
CR6	6	6	6	6	6	6	7

Section 2: Market Risk Measure

Part 1: Determine the PRIIP Category to select the applicable methodology





Step 1

To calculate the VaR Return Space using the Cornish Fisher expansion, you need the history of observed returns of the PRIIP. The returns are calculated by taking the natural logarithm of the price at the end of the current period divided by the price at the end of the previous period.

Zeroeth Moment (M₀): This is the number of observed returns.

First Moment (M₁): This is the average of the observed returns.

Second Moment (M_2): This is the average of the square of each return less M_1 . It summarises the variance or width of the distribution of the returns.

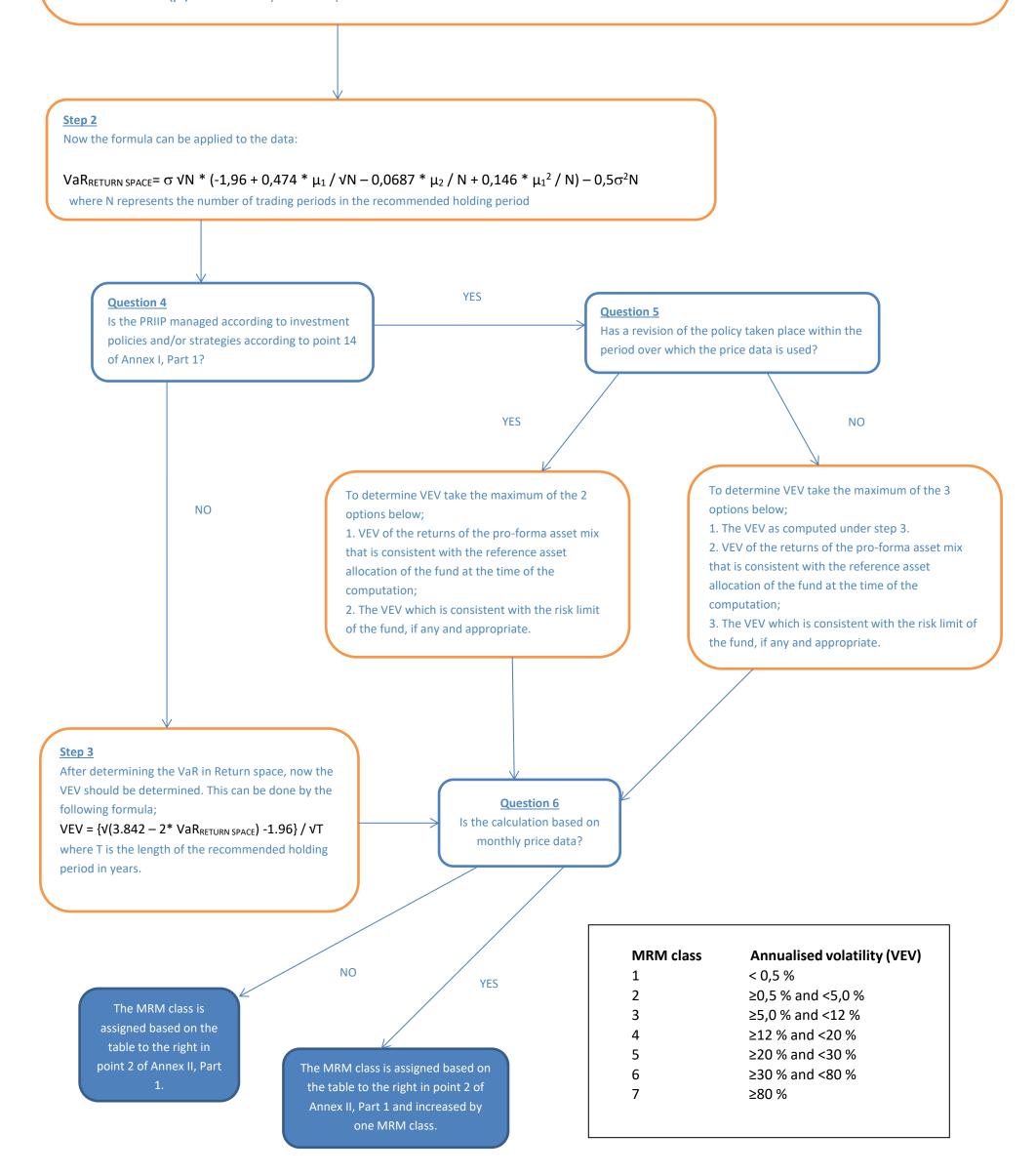
The standard deviation (σ) is the square root of M₂.

Third Moment (M₃): This is the average of the cube of each return less M₁. It summarises the asymmetry or skewness of the distribution of the returns.

The skew (μ_1) is M_3 divided by the cube of the standard deviation.

Fourth Moment (M₄): This is the average of the fourth power of each return less M₁. It summarises the extent of wider tails or kurtosis of the distribution of the returns.

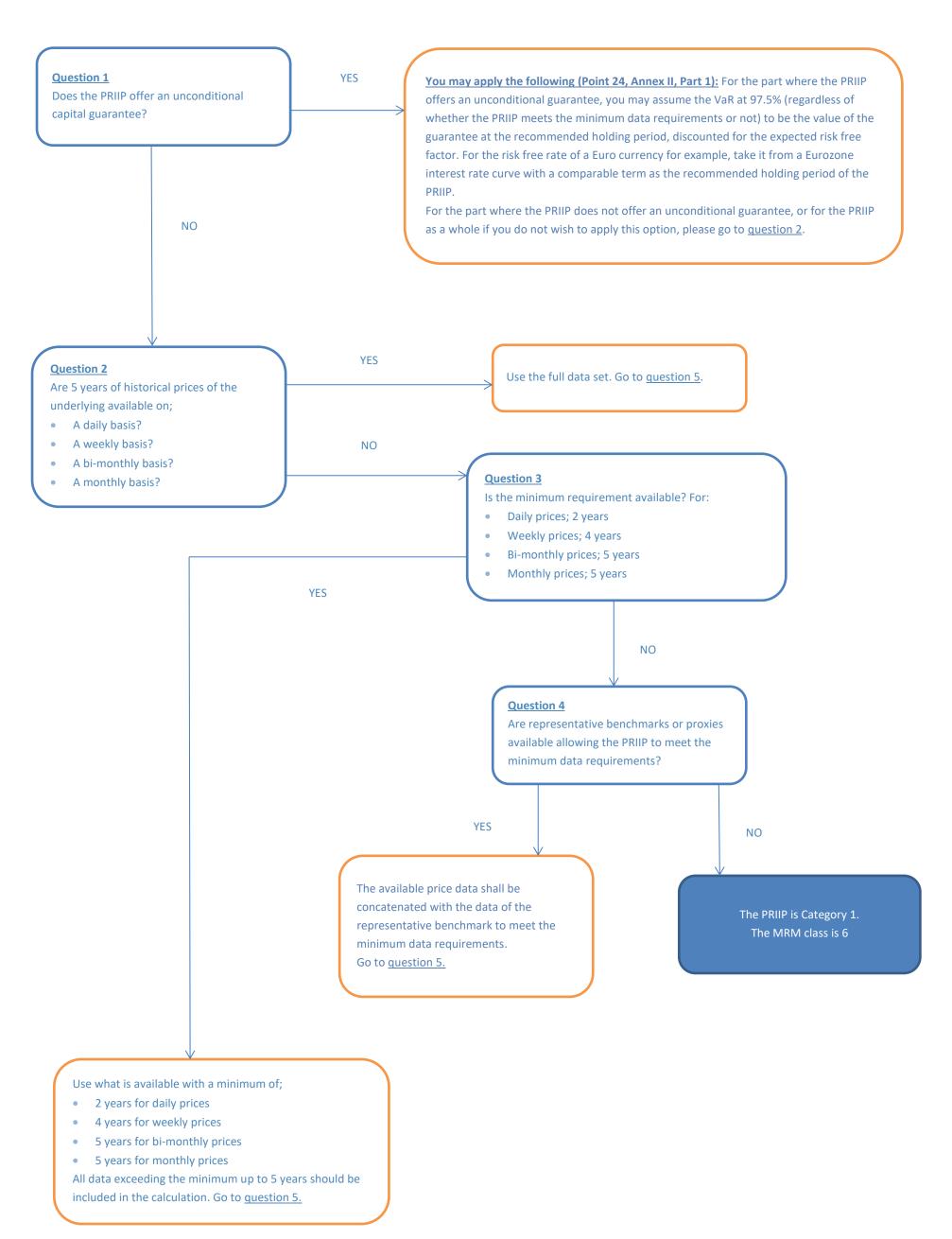
The excess kurtosis (μ_2) is M₄ divided by the fourth power of the standard deviation less 3

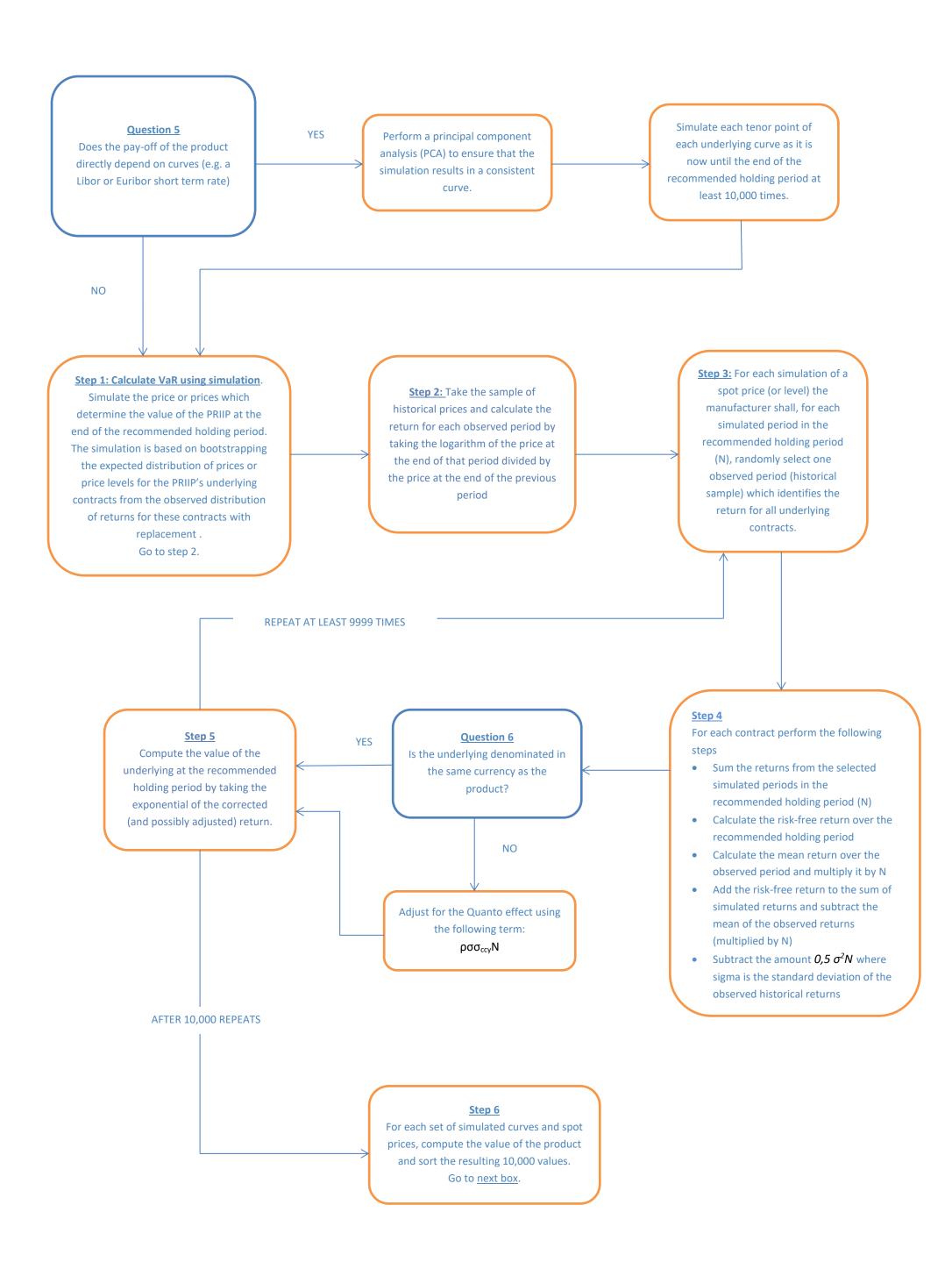


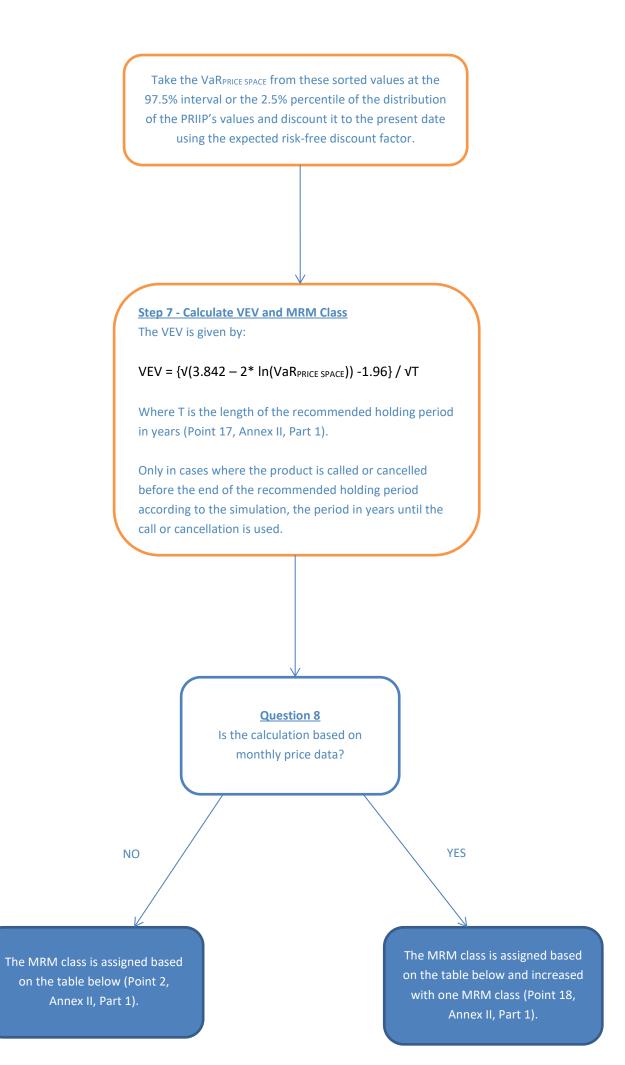
Calculation Example Category 2 PRIIPs

5 years of daily observed prices (Euro Stoxx 50 from 01.05.12 to 25.05.17)

Trading days per year M0 (under paragraph 10 of Annex II) M1	256 1280 0.0003389	365 (number of days) – 104 (number of weekend days) – 5 (public h Number of observations in the period 256*5=1280 Mean of all the observed returns in the sample (daily)	oolidays) = 256 days		
M2	0.000149905 Seco	nd Moment $M_2=\sum_i \frac{(r_i-M_1)^2}{M_0}=\sigma^2$	Volatility	0.0122435	$\sigma = \sqrt{M_2}$
M3	-6.44479E-07 Third	Moment $M_3 = \sum_{i} (r_i - M_1)^3 / M_0$	Skew	-0.35114343!	$5 \mu_1 = M_3 / M_2^{1,5}$
M4	1.46705E-07 Four	th Moment $M_4=\sum_i^r (r_i-M_1)^4/M_0$	Excess Kurtosis	3.52850338	$\mu_2 = (M_4/M_2^2) - 3$
Daily σ	0.01224357			$\sqrt{z_{\alpha}^2}$	- 2 * VaR _{Return Space} - z _σ
Confidence level	2.50%	Polynomial	Divisor	$VEV_{Return\ Space} = \frac{V}{V}$	$-2 * VaR_{Return Space} - z_{\sigma}$
z_{α}	-1.959963985	z^2-1	6		V I
Annualized Volatility (1Y) $\sigma\sqrt{N}$	19.59%	z^3-3z	24	72 5) + ln(VaD) a
$(z_{\alpha}^2-1)/6$	0.47357647	2z^3-5z	36	$VFV_{\rm D}$: $a = \frac{\sqrt{z_{\bar{\alpha}} - z_{\bar{\alpha}}}}{2}$	$2 * \ln(VaR_{Price\ Space}) - z_{\alpha}$
$(z_{\alpha}^{3}-3z_{\alpha})/24$	-0.068717874			V L V Price Space —	\sqrt{T}
$(2z_{\alpha}^{}3 - 5z_{\alpha})/36$	-0.146067276				
RHP (Recommended Holding Period expressed in years)	Number of Days	VaR (Return Space)	VEV Return Space	MRM class	VaR-equivalent volatility (VEV)
1	256	-0.4053	0.1969	1	<0,5%
3	768	-0.7247	0.1964	2	0,5%-5,0%
5	1280	-0.9566	0.1963	3	5,0%-12%
10	2560	-1.4081	0.1962	4	12%-20%
20	5120	-2.1029	0.1961	5	20%-30%
50	12800	-3.6764	0.1960	6	30%-80%
				7	>80%







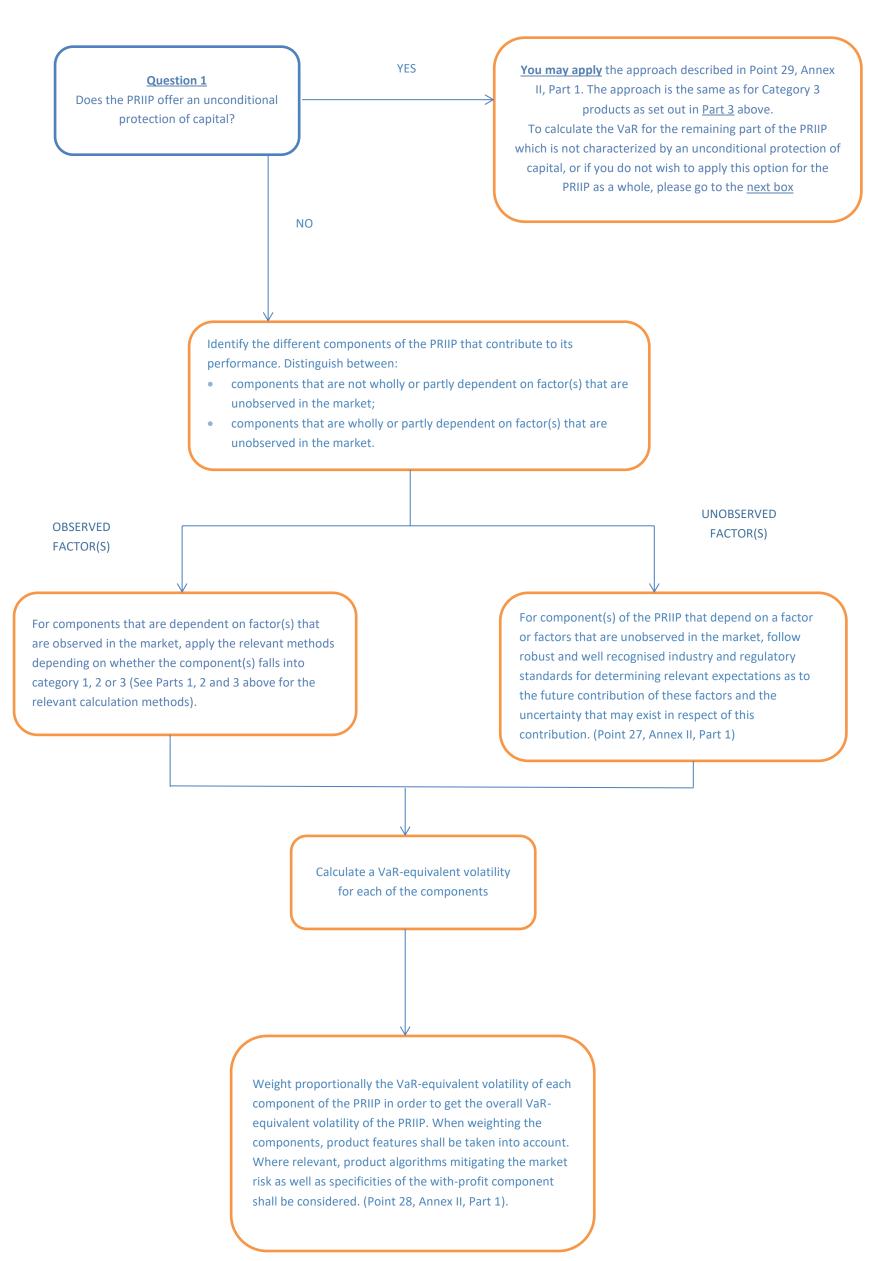
MRM class	Annualised volatility (VEV)
1	< 0,5 %
2	≥0,5 % and <5,0 %
3	≥5,0 % and <12 %
4	≥12 % and <20 %
5	≥20 % and <30 %
6	≥30 % and <80 %
7	≥80 %

<u>Steps 1-6</u>: 12 days RHP, 20 simulations, 1280 observed daily prices (5 years – Euro Stoxx 50 – from 01.05.12 to 28.04.17)

E)	(AMPLE SIMULATION: SIMULATION 1		DISTRIBUTIO	ON OF SIMUL	ATIONS
EACH SIMULATED PERIOD IN THE RHP (RHP=12 DAYS)	RANDOMLY SELECT ONE OBSERVED PERIOD OVER 1280 PERIODS (5*256)	RETURN FOR ALL UNDERLYING CONTRACTS	SIMULATIONS	RANK	VALUE
	1 754	0,003144319	1	9	0,9784144
	2 247	0,000786848	2	1	1,05729999
	3 840	-0,034100705	3	15	0,9277006
	4 137	1,21011E-05	4	14	0,93097185
	5 117	0,012355476	5	12	0,94650357
	6 524	-0,000889222	6	6	0,99116702
	7 195	0,002623287	7	17	0,92026668
	8 138	0,000278285	8	8	0,97890466
	9 457	0,014583841	9	3	1,01099443
1	0 717	0,001495982	10	2	1,01111948
1	1 809	-0,01294047	11	5	0,99193409
1	2 259	-0,00477314	12	19	0,91167231
			13	10	0,95711822
Return = E[Retur]	$n_{risk-neutral}$] - $E[Return_{measured}]$ - 0	$,5\sigma^2N- ho\sigma\sigma_{ccy}N$	14	4	0,99512444
			15	18	0,91342991
$E[Return_{risk-neut}]$	$_{ral}] = Riskfree Return + Sum of simu$	ılated returns	16	7	0,98975916
			17	20	0,90900029
RISK-FREE RETURN OVER THE RHP	0,000568027		18	11	0,94922686
SUM OF SIMULATED RETURNS	-0,017423398		19	13	0,93321018
E[RETURN risk-neutral]	-0,016855371		20	16	0,92273156
E [RETURN MEASURED]	0,004067173				
0,5 σ2 N	0,00089943				
ADJUSTED SIMULATED RETURN:	-0,021821974				
EXP of SIMULATED RETURN	0,978414403				
RHP LENGTH:	12 DAYS				

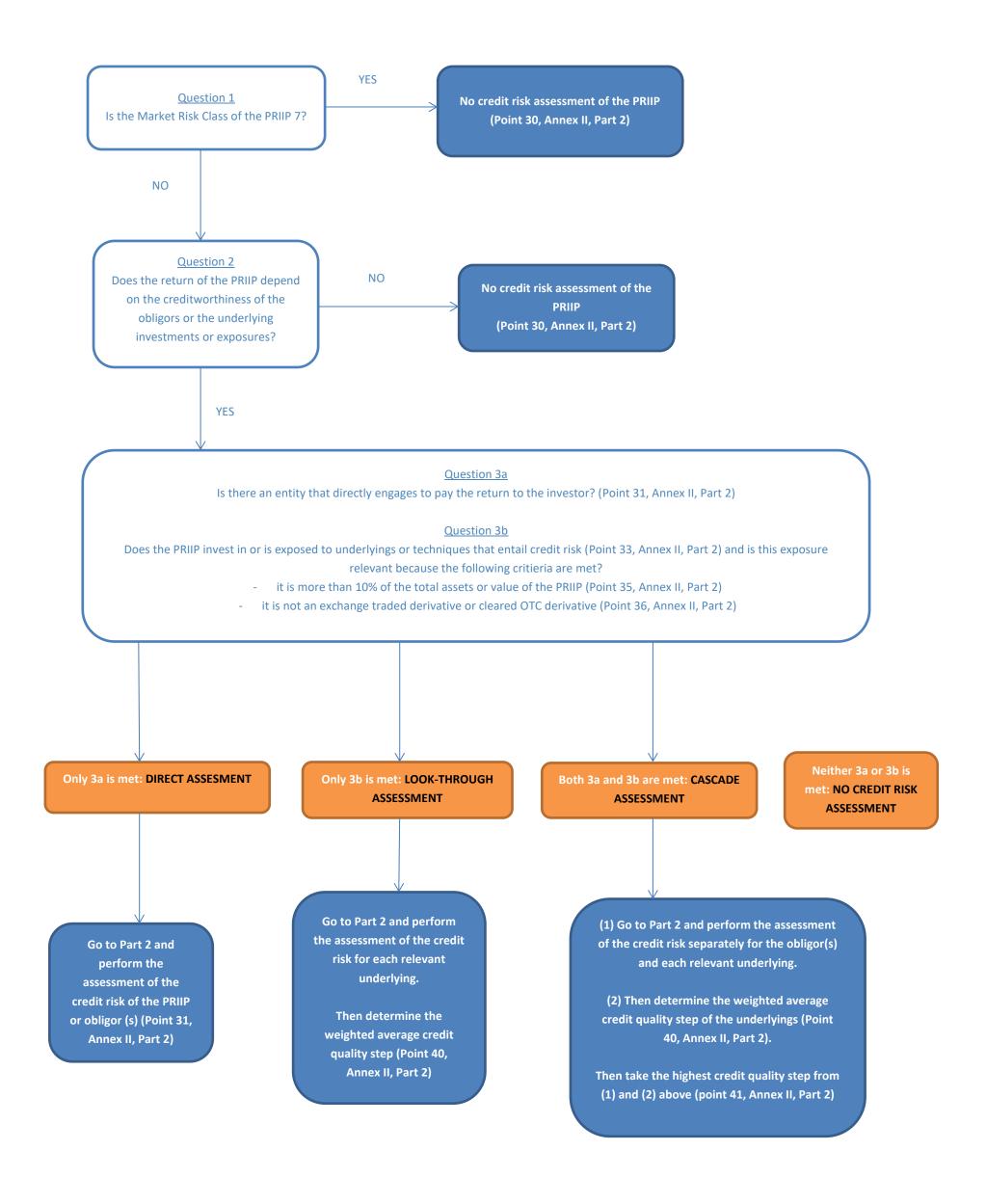
Step 7: RHP = 1 AND 3 YEARS, 1000 simulations, 1280 observed daily prices (5 years – Euro Stoxx 50 – from 01.05.12 to 28.04.17)

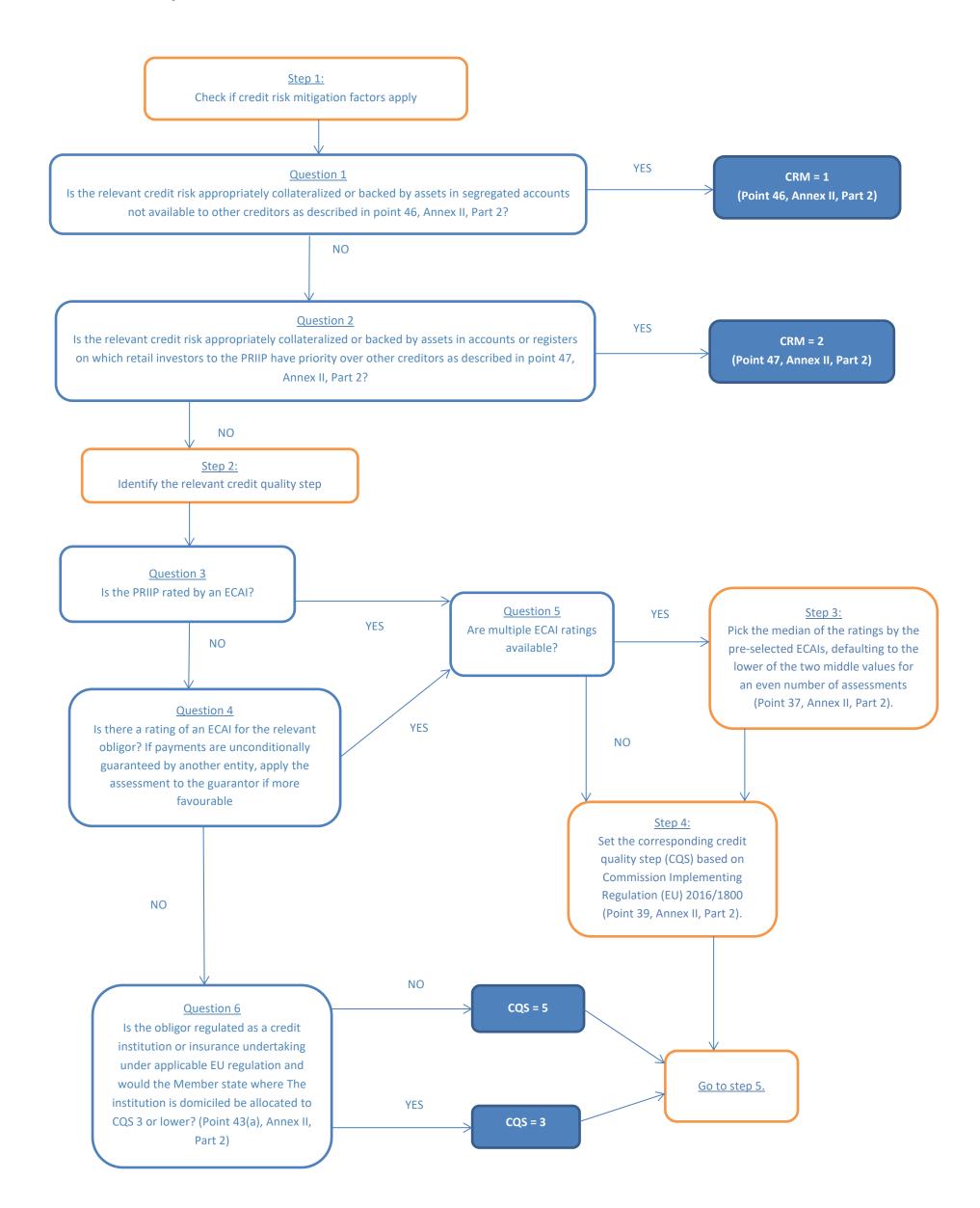
U UUU338031	
0,01224357	
1280	
1.2	
2,3	
256	
-1,95996398	
975	
т)	
1	3
0,6832	0,4957
0,1856	0,1907
	1,2 2,5 256 -1,95996398 975 T) 1



Section 3: Credit Risk Measure

Part 1: Should credit risk be assessed and if so how





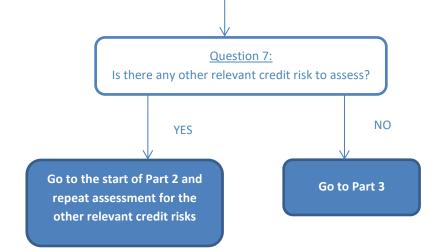
<u>Step 5: Allocation of credit assessment corresponding to the credit quality steps</u>

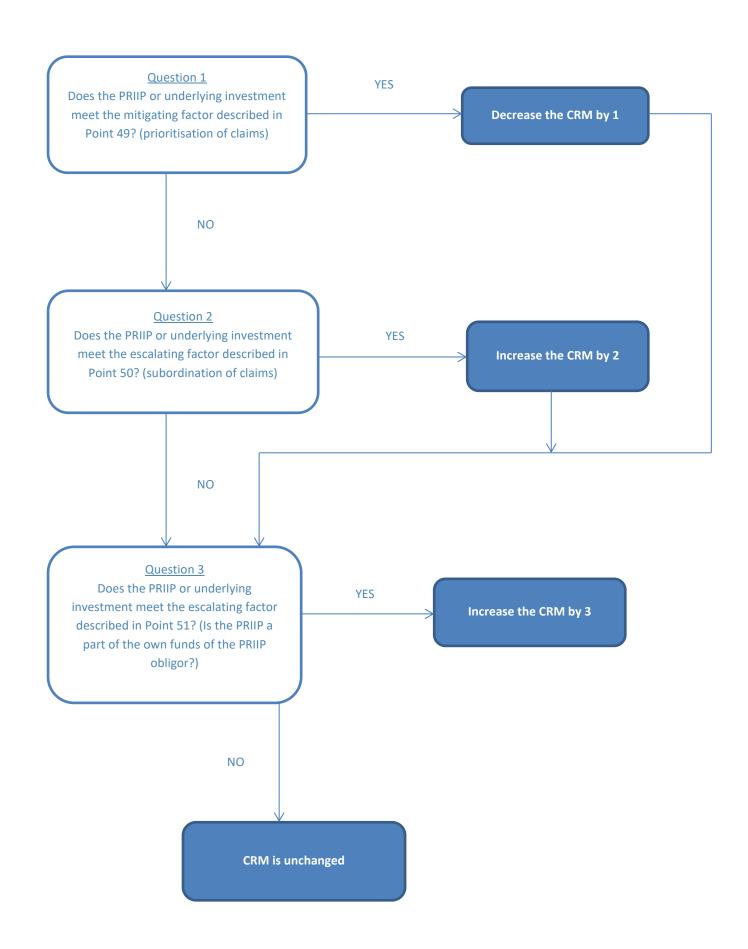
Adjust the CQS depending on the term of the PRIIP according to the table below in point 42, Annex II, Part 2 unless the credit assessment assigned reflects the term of the PRIIP.

Credit quality step	Adjusted credit	Adjusted credit	Adjusted credit
pursuant to point 38	quality step, in the	quality step, in the	quality step, in the
of this Annex	case where the	case where the	case where the
	maturity of the	maturity of the	maturity of the
	PRIIP, or its	PRIIP, or its	PRIIP, or its
	recommended	recommended	recommended
	holding period where	holding period where	holding period where
	a PRIIP does not	a PRIIP does not	a PRIIP does not
	have a maturity, is up	have a maturity,	have a maturity,
	to one year	ranges from one year	exceeds twelve years
		up to twelve years	
0	0	0	0
1	1	1	1
2	1	2	2
3	2	3	3
4	3	4	5
5	4	5	6
6	6	6	6

Step 6
Convert the CQS into a CRM measure according to the table below in point 45, Annex II, Part 2

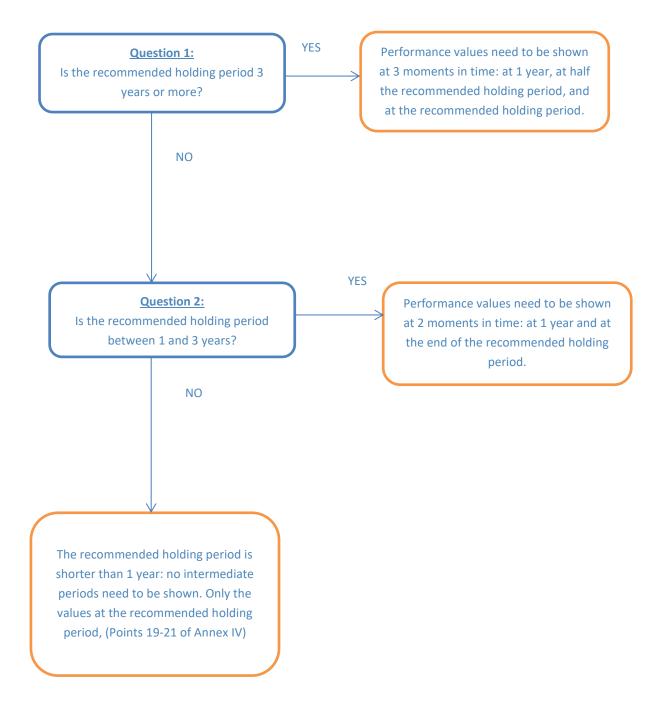
Adjusted credit quality step	Credit risk measure
0	1
1	1
2	2
3	3
4	4
5	5
6	6

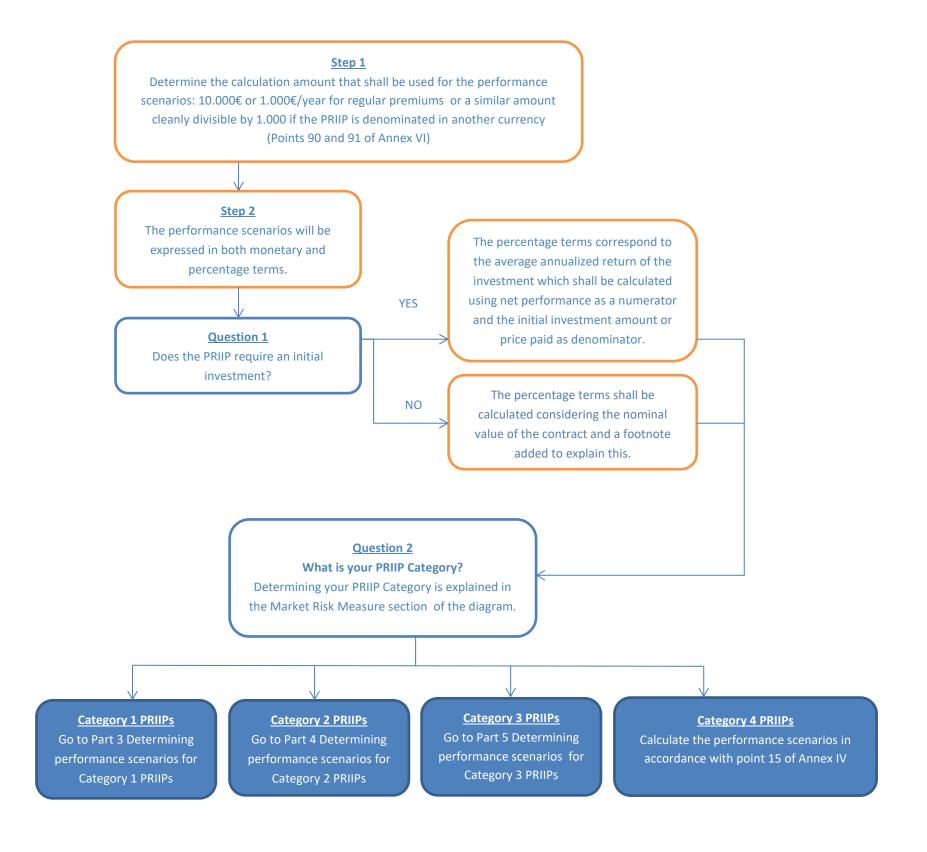


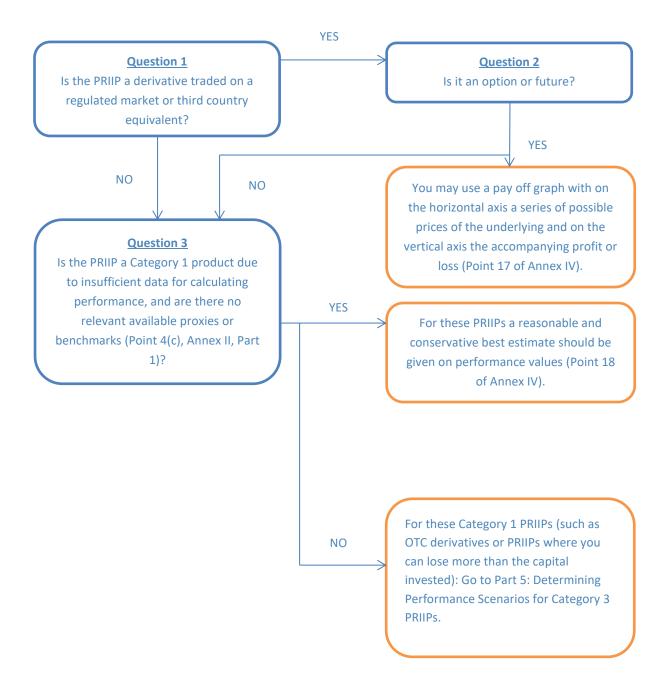


B. Performance Scenarios

Part 1: Determining the holding periods that need to be shown







a) Performance calculations for the unfavourable, moderate and favourable scenarios

The items listed below are needed in order to calculate the **performance values for the relevant holding period**. Most values are known already from the calculation for MRM, except for N.

The values for the recommended holding period and the intermediate holding periods are calculated by the same formulas as displayed below, changing only N which is different at the recommended holding period compared to the intermediate holding periods.

- N is the number of trading days, weeks or months within the holding period. So for a Recommended Holding Period of 5 years and If there is daily price data N= 5*~252 = 1260;
 - Exp the exponential of;
- M₁- the mean of the distribution of all the observed returns in the historical period;
 - \bullet $\sigma-$ standard deviation or volatility of the distribution;
 - μ_1 skew of the distribution;

 $\bullet \mu_2$ - the excess kurtosis of the distribution.

Unfavourable scenario;

$$\begin{split} & Exp \; [\; M_1*N + \sigma \; \sqrt{N} \; * \; (-1.28 \; + \\ & 0.107 \; * \; \mu_{_1} / \; \sqrt{N} + 0.0724 \; * \; \mu_{_2} / \; N \\ & - 0.0611 \; * \; \mu_{_1}{}^2 / \; N) - 0.5\sigma^2 N \;] \end{split}$$

Moderate scenario;

Exp [$M_1*N - \sigma \mu_1/6 - 0.5\sigma^2N$]

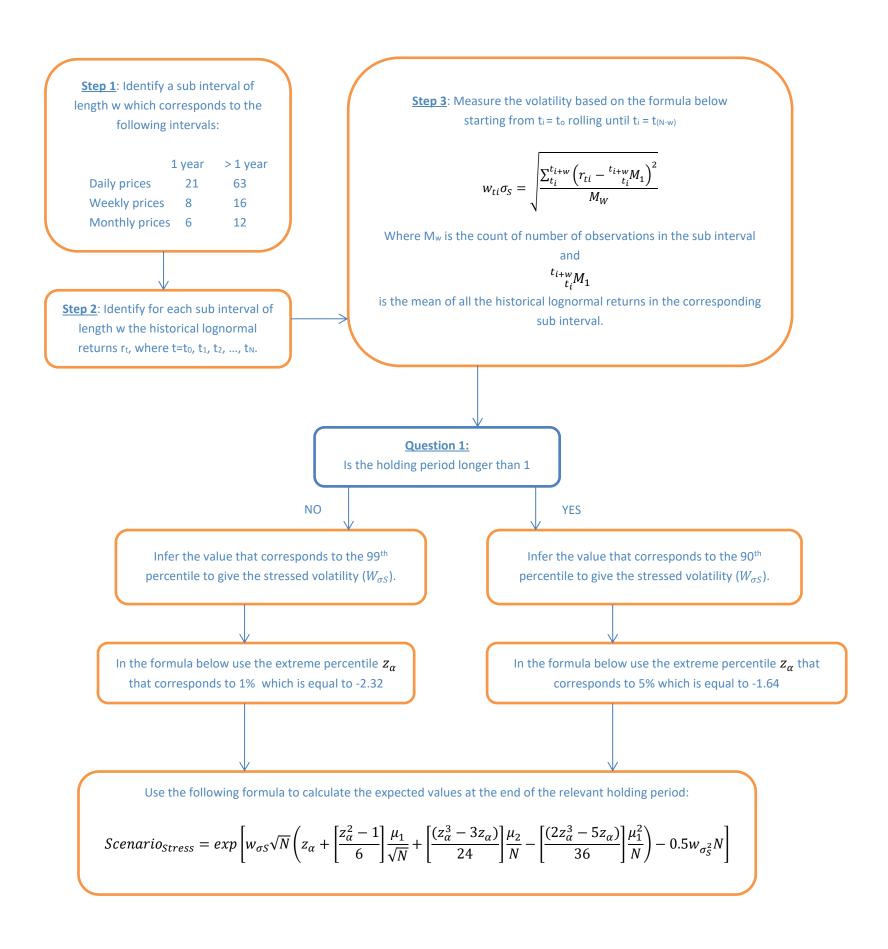
Favourable scenario;

Exp [$M_1*N + \sigma \sqrt{N} * (1.28 + 0.107 * \mu_1 / \sqrt{N} - 0.0724 * \mu_2 / N + 0.0611 * \mu_1^2 / N) - 0.5\sigma^2 N$]

5 years of observed daily prices (Euro Stoxx 50 – from 01.05.12 to 25.05.17), RHP 1, 3 and 5 years , examples considering an investment amount of 1 €

	α	z_{lpha}	$(z_{\alpha}^2 - 1)/6$	$(z_{\alpha}^3-3z_{\alpha})/24$	$(2z_{\alpha}^3 - 5z_{\alpha})/36$
Unfavorable Scenario - Critical values	10%	-1,281551566	0,107062403	0,072494466	0,061060634
Moderate Scenario - Critical values	50%	0	-0,16666667	0	0
Favorable Scenario - Critical values	90%	1,281551566	0,107062403	-0,072494466	-0,061060634

	Standard Performance Scenarios			
		RHP		
	RHP	5 years	1 year	3 years
N is the number of trading periods in the recommended holding period		1280	256	768
$\sigma\sqrt{N}$		0,438039282	0,195897122	0,339303769
Unfavorable scenario		0,799432892	0,832148758	0,792589109
Moderate scenario		1,402994819	1,070681172	1,225626426
Favorable scenario		2,456450066	1,374349473	1,890801557



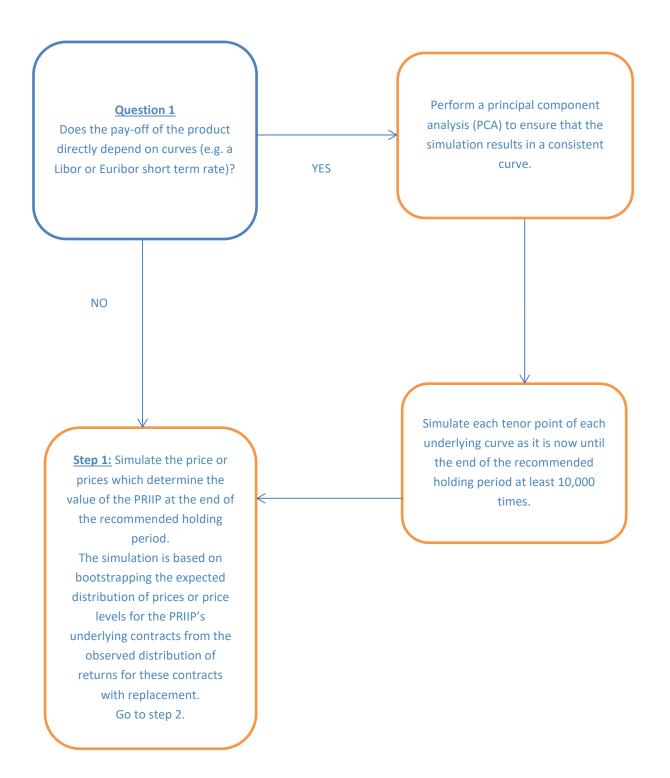
RHP 1, 3 and 5 years, 5 years of daily observed prices (Euro Stoxx 50 – from 01.05.12 to 25.02.17)

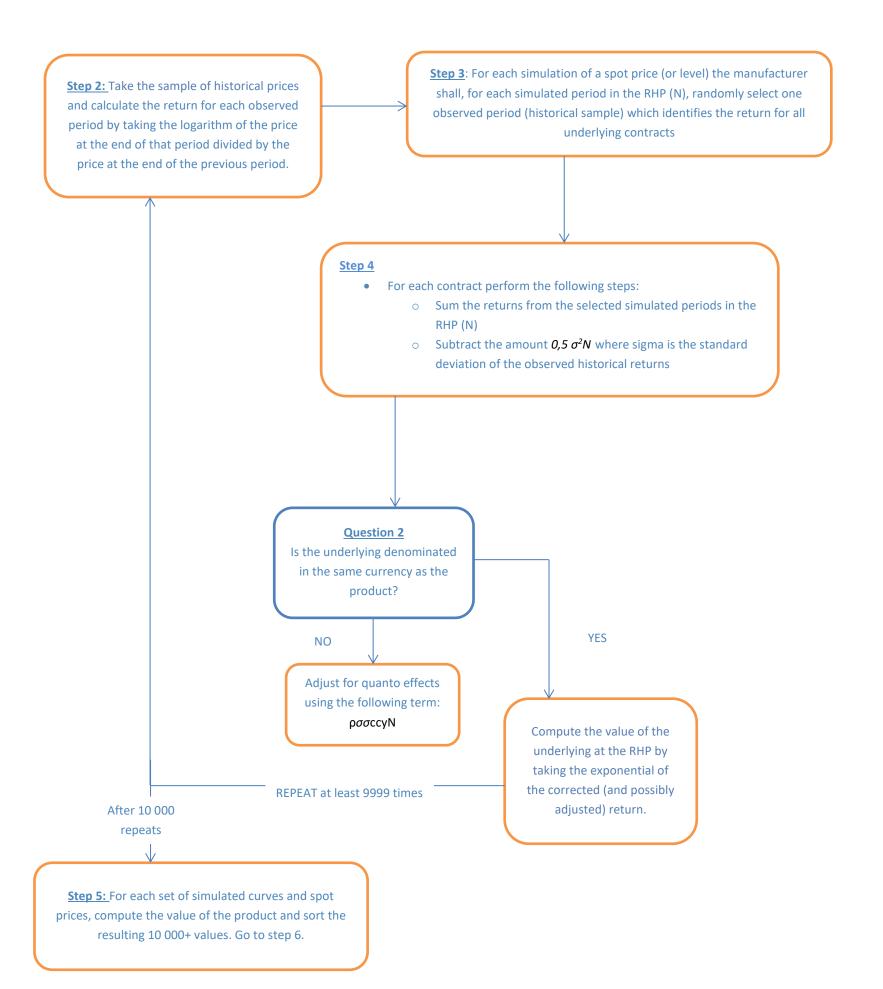
		Stressed Performance Scenario			
	α	z_lpha	$(z_{\alpha}^2-1)/6$	$(z_{\alpha}^3 - 3z_{\alpha})/24$	$(2z_{\alpha}^3 - 5z_{\alpha})/36$
RHP 1 YEAR - Annex IV, point 11	1%	-2,326347874	0,735315739	-0,233787728	-0,376337746
RHP OTHER HOLDING PERIODS - Annex IV, point 11	5%	-1,644853627	0,284257242	0,020180747	-0,018782716
Stressed volatility 1 year - Annex IV, point 10(d)	0,025767278				
Stressed volatility 3 years - Annex IV, point 10(d)	0,017657123			RHP	
Stressed volatility 5 years - Annex IV, point 10(d)	0,017152366		5 years	1 year	3 years
N is the number of trading periods in the recommended ho	olding period		1280	256	768
$W_{\sigma_S}\sqrt{N}$			0,613661699	0,412276441	0,489328534
STRESSED SCENARIO			0,301389802	0,349241623	0,396012057

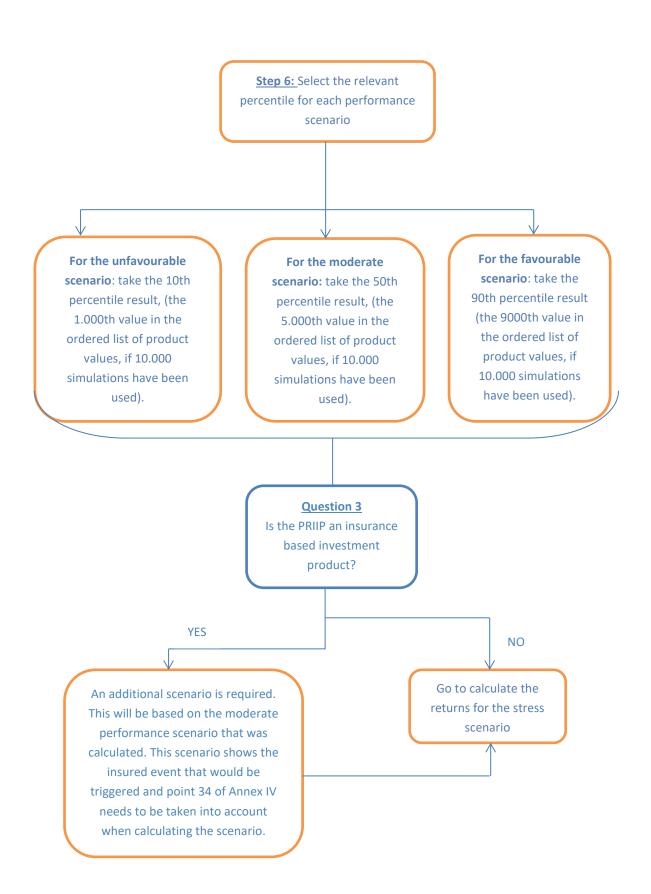
Part 5: Determining Performance Scenarios for Category 3 PRIIPs

Please note that the performance scenarios hinge on the same simulated data as the MRM calculations, hence manufacturers are not required to make a new simulation when switching from the MRM to the Performance Scenarios calculations. However, the complete process for the performance scenarios is described in this Part for the sake of clarity.

a) Performance calculations for the unfavourable, moderate and favourable scenarios







1000 simulations, RHP 1 and 3 years, 5 years of daily observed prices (Euro Stoxx 50 from 01.05.12 to 28.04.17)

Recommended holding period in years (T)							
		P	ercentile	Rank (over 1000 simulations)			
Used Rank Unfavo	urable scenario	10	Oth	900			
Used Rank Modera	Used Rank Moderate scenario			500			
Used Rank Favoura	Used Rank Favourable scenario		Oth	100			
V54.50	_						
YEARS	1	3					
Unfavorable Scenario	0,848537 0,7	80318	The scenario	s values under different performance s	cenarios shall be		
Moderate Scenario	1,086382 1,2	23794	calculated i	in a similar manner as the market risk m	easure (MRM) -		
Favourable Scenario	1,39373 1,9	36616	Poi	nt 4 Annex IV and Point 12 letter a, b An	nex IV)		

b) Performance calculations for the stress scenario

<u>Step 1</u>: Identify a sub interval of length w which corresponds to the following intervals:

1year> 1 yearDaily prices2163Weekly prices816Monthly prices612

Step 2: Identify for each sub interval of length w the historical lognormal returns rt, where t=t0, t1, t2, ..., tN.

Step 3: Measure the volatility based on the formula below starting from $t_i = t_0$ rolling until $t_i = t_{(N-w)}$

$$w_{ti}\sigma_{S} = \sqrt{\frac{\sum_{t_{i}}^{t_{i+w}} \left(r_{ti} - \frac{t_{i+w}}{t_{i}} M_{1}\right)^{2}}{M_{W}}}$$

Where $M_{\mbox{\tiny W}}$ is the count of number of observations in the sub interval and

$${}^{t_{i+w}}_{t_i}M_1$$

is the mean of all the historical lognormal returns in the corresponding sub interval.

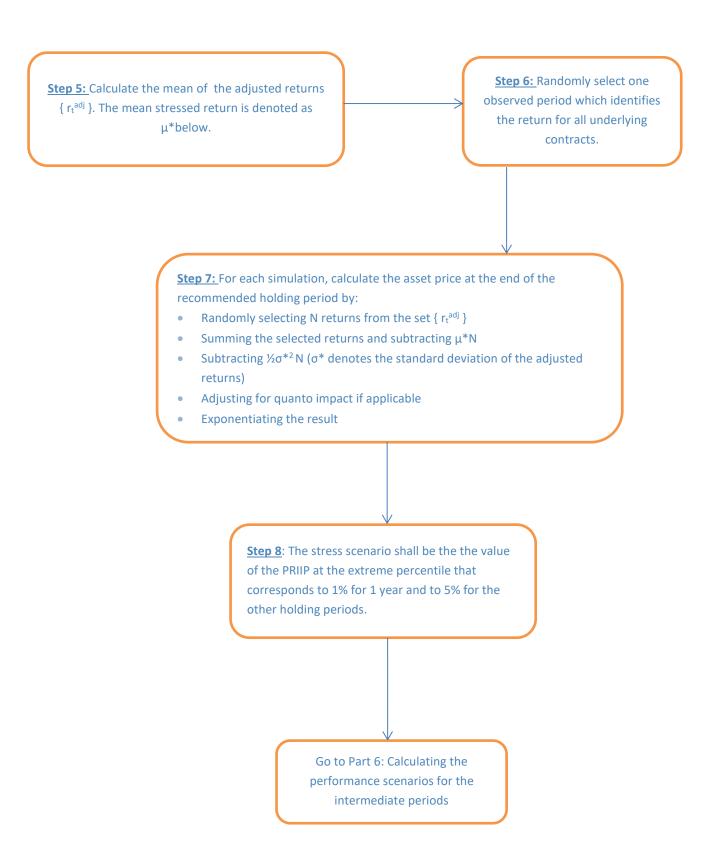
Infer the stressed volatility $W_{\sigma S}$ that corresponds to the 99th percentile for 1 year and the 90th percentile for the other holding periods

Step 4: Rescale historical returns r_t, based on the formula set out below

$$r_t^{adj} = r_t * \frac{{}^W \sigma_S}{\sigma_S}$$

where $\sigma_{\!S}$ is the standard deviation of the observed historical returns

Go to step 5.



Steps 1-3: 1000 simulations, RHP of 2 years

RECOMMENDED HOLDING PERIOD = N = 2 YEAR = 512 OBS W=63 days

Starting from ti=t0 rolling until ti=t(N-w)=512-63=449

		vv – os days					
DATE	PRICE		OBSERVED RETURNS	N		Rolling volatility	
04/05/2015	3632,94				t_0		
05/05/2015	3546,56	r_{1}	-0,024064118	1	t_1	0,011821003	
06/05/2015	3558,03	r_2	0,003228901	2	t_2^-	0,010212764	
07/05/2015	3556,21	r_3	-0,00051165	3	t_3	0,010615001	
08/05/2015	3649,48	•	0,025889321	4	•	0,011073765	
11/05/2015	3624,41		-0,006893175	5	•	0,00829045	
12/05/2015	3573,1		-0,01425795	6	•	0,00849749	
13/05/2015	3553,42		-0,005523046	7	•	0,00737515	
14/05/2015	3602,22		0,013639802	8	•	0,007389004	
15/05/2015	3573,07		-0,008125152	9	•	0,012145054	
					•		
23/01/2017	3273,04		-0,002604259	445		0,009510134	
24/01/2017	3281,53		0,009160707	446		0,009459426	
25/01/2017	3326,15		-0,002328776	447		0,009354546	
26/01/2017	3319,13		-0,002037409	448	- 10 - 10	0,009401931	
27/01/2017	3303,33	$r_{T-w} = 512 - 63 = 449$	0,008093104	449	$t_{T-w} = 512 - 63 = 449$	0,009386922	

Step 4: 1000 simulations, RHP of 2 years

DATE	Rank	Rolling volatility		Stressed returns
04/05/2015	38	0,010556603	Percentile RHP > 1	$r_t^{adj} = r_t * \frac{w_{\sigma S}}{\sigma} -0.04568$
05/05/2015	57	0,009673011	95	σ_{s} -0,02817
06/05/2015	56	0,009676026		0,001279
07/05/2015	55	0,00967635	Inferred volatility (RHP > 1 year)	-0,00281
08/05/2015	50	0,009972533	0,018101868	0,015142
11/05/2015	49	0,01006383		0,018321
12/05/2015	45	0,010207575	W_{σ_S}	-0,01762
13/05/2015	34	0,01152721		-0,01695
14/05/2015	32	0,012145054		0,016882
15/05/2015	31	0,012591142		-0,00417
18/05/2015	29	0,01293892		-0,01061
19/05/2015	30	0,012933856	Used rank (RHP > 1)	0,014619
20/05/2015	28	0,013087051	45	-0,02976
•				•
			Observed Standard Deviation	•
•			0,013630478	•
•				•
25/04/2017		3583,16		0,021522
26/04/2017	•	3578,71		-0,00547
27/04/2017	•	3563,29		-0,00479
28/04/2017	r_{T-w}	3559,59		0,019014

Steps 5-6: 1000 simulations, RHP of 2 years

SIMULATED RETURNS IN THE RHP (RHP=512 DAYS = 2 YEARS)												
DAY	1	2	3	•	•	•	509	510	511	512		Sum of stressed returns
Simulation 1	0,027392	0,014038	-0,2117	•			0,008783	0,01293	0,026752	0,01903		1,056163
Simulation 2	-0,00293	-0,01822	-0,01513	•			-0,00293	0,003203	-0,01623	-0,00621		0,371867
Simulation 3	0,015496	-0,001	-0,01035	•			0,029695	0,006496	-0,00374	0,011948		0,464389
Simulation 4	-0,02976	0,02458	0,011466	•			0,001153	0,026313	-0,01102	-0,00943		0,542711
	•		•		•	•	•			•		•
	•	•	•	•	•	•	•	•	•	•		•
•	•	•	•	•	•	•	•	•	•	•		•
Simulation 997	0,038841	0,008783	-0,01705	•	•	•	-0,00612	0,029132	-0,03364	-0,00746		0,399851
Simulation 998	-0,01503	-0,00293	0,007265	•			0,024164	-0,03123	-0,02629	-0,00383		0,144918
Simulation 999	-0,01903	0,029695	0,007654	•	•		-0,00612	0,02476	0,006858	0,054131		0,65239
Simulation 1000	0,017111	0,001153	-0,00915	•	•	•	-0,00374	0,011466	0,029465	-0,00612		-0,31238

Steps 7-8: 1000 simulations, RHP of 2 years

	Sum of stressed r	eturns	Simulated stressed returns	Rank	Simulated stressed prices
Simulation 1	0,547871		-0,308473702	716	0,734567
Simulation 2	0,23742	$E[Return_{MEASURED}] = N\mu^*$	0,036099698	380	1,036759
Simulation 3	0,11592	0,376425586	0,209019028	236	1,232468
Simulation 4	0,526658		-0,145282546	570	0,864778
Simulation 5	0,388818		0,500883786	68	1,650179
	•		•	•	•
Simulation 997	0,423087		-0,057786731	512	0,943851
Simulation 998	0,26424		-0,046921846	500	0,954162
Simulation 999	0,030446		0,222387303	251	1,249055
Simulation 1000	-0,20313		-0,66079576	904	0,51644



	Percentile stressed scenario	Rank Stressed Scenario	Stressed Scenario
	z_{lpha}		
RHP = 2 Y (512 days)	5	950	0,488090936

